

The rules of derivative:

- i. $\frac{d}{dx}(f(x) + g(x)) = f'(x) + g'(x)$. (sum rule)
- ii. $\frac{d}{dx}(f(x) - g(x)) = f'(x) - g'(x)$. (difference rule)
- iii. $\frac{d}{dx}(f(x) \cdot g(x)) = f'(x) \cdot g(x) + f(x) \cdot g'(x)$. (product rule)
- iv. $\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{f'(x) \cdot g(x) - f(x) \cdot g'(x)}{[g(x)]^2}$. (quotient rule)
- v. $\frac{d}{dx}(cf(x)) = c \frac{d}{dx}(f(x)) = cf'(x)$. (constant multiple rule)
- vi. $\frac{d}{dx}(c) = 0$. (Constant function).
- vii. $\frac{d}{dx}(x) = 1$.
- viii. $\frac{d}{dx}(x^n) = nx^{n-1}$, where $n \in \mathbb{R}$.

Derivatives of Trigonometric Functions:

$f(x)$	$\sin(x)$	$\cos(x)$	$\tan(x)$	$\cot(x)$	$\sec(x)$	$\csc(x)$
$f'(x)$	$\cos(x)$	$-\sin(x)$	$\sec^2(x)$	$-\csc^2(x)$	$\sec(x) \cdot \tan(x)$	$-\csc(x) \cdot \cot(x)$

Derivatives of Inverse Trigonometric Functions:

- i. $\frac{d}{dx}(\sin^{-1}(x)) = \frac{1}{\sqrt{1-x^2}}$.
- ii. $\frac{d}{dx}(\cos^{-1}(x)) = \frac{-1}{\sqrt{1-x^2}}$.
- iii. $\frac{d}{dx}(\tan^{-1}(x)) = \frac{1}{1+x^2}$.
- iv. $\frac{d}{dx}(\cot^{-1}(x)) = \frac{-1}{1+x^2}$.
- v. $\frac{d}{dx}(\sec^{-1}(x)) = \frac{1}{x\sqrt{x^2-1}}$.
- vi. $\frac{d}{dx}(\csc^{-1}(x)) = \frac{-1}{x\sqrt{x^2-1}}$.

Derivatives of exponential Functions:

- i. $\frac{d}{dx}(e^x) = e^x$.
- ii. $\frac{d}{dx}(a^x) = a^x \cdot \ln a$.

Derivatives of logarithmic Functions:

i. $\frac{d}{dx}(\ln(x)) = \frac{1}{x}$.

ii. $\frac{d}{dx}(\log_a x) = \frac{1}{x \cdot \ln a}$.

The Chain Rule:

If $F(x) = (f \circ g)(x) = f(g(x))$ then $\frac{dF}{dx} = f'(g(x)) \cdot g'(x)$